

... for a brighter future



Argonne



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 $G_r(r) = 1 + \frac{1}{2r^2 e^r} \int QS(Q) \sin(Qr) dQ$ THEN A MIRACLE OCCURS ....

"I think you have to be a bit more explicit here in step two"

#### **Pair Distribution Function Analysis**

Chris Benmore X-ray Science Division, Argonne National Lab.



## Pioneers in the history of PDF

*X-ray determination of the Structure of Glass Warren BE. J. Am. Ceram. Soc. 17 (1934) 249.* 

*The partial structure factors of liquid Cu-Sn* Enderby JE, North DM and Egelstaff PA. Phil. Mag. 14 (1966) 961.



FIG. 1.—Vacuum camera with monochromator for making X-ray diffraction patterns of glass.



**Bertram Warren** 



John Enderby



Peter Egelstaff



## Types of Disorder





## Order within Disorder



#### A formation of skydivers illustrates order on an intermediate length scale.

P.S. Salmon Nature Materials 1, 87-88 (2002)

"Each diver has a simple set of rules for bonding to the next, but there is sufficient flexibility for different patterns of ordering to be created on the scale of a few body lengths." Faber-Ziman formalism – element specific



S<sub>Number-Concentration</sub>(Q)

# PDF in context with other common methods

Simulation

#### Experiment

Neutrons/X-ray PDF	Good AVERAGE overview of structure Short range order (SRD) Medium range order (MRD) Neutron Diffraction Isotope Substitution	<b>Inverse Methods:</b> Reverse Monte Carlo (RMC) Empirical Potential	Perfect fits to PDF data No predictive power Many constraints essential !
Crystallography	Long Range Order (LRO)	Structure Refinement (EPSR)	
EXAFS, XANES	SRO, Element Specific, Small concs.	Classical Molecular Dynamics	Essential physics, trends Fit to PDF sometimes poor
Anomalous x-ray	SRO, MRO. Element specific, Difficult to do accurately	<i>Ab initio</i> simulations Density Functional	Accurate predictions Box size limit ?
Vibrational Spectroscopy	Inelastic N and X, Raman and Infrared. SRO, MRO. Need good structural model.	Theory (DFT)	
NMR	Isotope Specific. Speciation $Q_{n.}$		



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## Monochromatic PDF versus time-of-flight PDF



Chapter 12: Structure of glasses and melts in "Neutron Scattering in Earth Sciences". Reviews in Mineralogy and Geochemistry. 63 (2006) 375-311.



#### $S(\Omega,\omega)$ cuts along a liquid structure factor





### Neutron and X-ray differential cross sections

#### Neutron

X-ray





## Neutron and X-ray Static Structure Factors





#### Neutron and X-ray differential cross sections





# Outline of time-of-flight neutron analysis procedure





#### Neutron diffraction corrections



Ideal neutron PDF experiment designed so that attenuation and multiple scattering effects are ~10%



### How do the corrections effect the measured data ?



*Time-of-Flight Neutron Total Scattering Data Analysis implemented in the software suite ISAW.* Nucl. Instrum. Methods. A 562 (2006) 422-432.



## Proton recoil and Vanadium normalization







## Interpreting Structure Factors

Tetrahedral glasses r<sub>1</sub>=first peak position in real space

FSDP – First Sharp Diffraction Peak : Intermediate Range Order

SSDP –Second Sharp Diffraction Peak : Extended Range Order



Phys. Rev. B. 72 (2005) 132201.



## Weighted Partial Structure Factors





## The Miracle step



Truncate at a positive node to minimize Fourier artifacts



#### A question of resolution – the effect of Qmax



J. Non-Cryst. Sol 111 (1989) 123.







### Flaw of Averages

PDF measures the AVERAGE structure i.e. coordination number





# Naturally occurring nuclides for NDIS

Identified by feasibility of Neutron Diffraction Isotopic Substitution experiment



First order difference  $\Delta b > 1 \text{ fm}$ Feasible using NOMAD at SNS Other

J. Enderby. World Scientific p16. ISBN 981-02-1463-4.



## Partial Structure Factors for glassy SiO<sub>2</sub>



Phys. Rev. B. 78 (2008) 144204 .



#### Partial Pair Distribution Functions of vitreous Silica





# H/D substitution : Partial Structure Factors for water





## Solving the Nanoproblem



Nature 440 (2006) 655.



# High energy x-ray beamlines at APS











#### Nanoscale Ordered MAterials Diffractometer



Courtesy of Joerg Neuefeind

#### Online in 2011

	D4c (ILL)	GEM (ISIS)	DRACULA (ILL Project)	NOMAD Project
Time averaged flux (10 <sup>8</sup> n/cm <sup>2</sup> )	0.4	~0.02	~1	~1.7 (1.4MW)
Detector coverage (strad)	0.11	4.0	1.5	~10
Product (10 <sup>6</sup> )	4.4	8	150	1700



#### Anomalous neutron diffraction - new possibilities at SNS

<sup>1</sup> H																	<sup>2</sup> He
Ľ	$\stackrel{_4}{\operatorname{Be}}$											5 B	ĉ	Ň	ð	۴	Ne
Na	<sup>12</sup> Mg											AI	14 Si	15 P	16 S	17 Cl	Ar
19 K	Ca <sup>20</sup>	Sc 21	<sup>22</sup> Ti	23 V	Cr	<sup>25</sup> Mn	Fe <sup>26</sup>	27 Co	28 Ni	Cu 29	<sup>30</sup> Zn	Ga 31	Ge	33 As	Se	<sup>35</sup> Br	36 Kr
<sup>37</sup> Rb	<sup>38</sup> Sr	<sup>39</sup> Y	<sup>40</sup> Zr	<sup>41</sup> Nb	42 Mo	43 Tc	Ru 44	<sup>45</sup> Rh	Pd <sup>46</sup>	Åg	48 Cd	49 In	Sn	Sb 51	Te <sup>52</sup>	53 	Xe
$\overset{55}{\text{Cs}}$	Ba 56	La 57	72 Hf	73 Ta	74 W	Re 75	76 Os	77 Tr	78 Pt	<sup>79</sup> Au	<sup>80</sup> Hg	<sup>81</sup> TI	Pb	83 Bi	<sup>84</sup> Po	At 85	86 Rn
B7 Fr	<sup>88</sup> Ra	89 Ac	 104 Rf	<sup>105</sup> Ha	106	107	108	109	110	111	112	113	114	115	116	117	118

	Če	Pr Pr	$\overset{60}{\text{Nd}}$	Pm	Sm Sm	63	Gd Gd	$\overset{65}{\text{Tb}}$	66 Dy	H0		Tm	70 Yb	
**	<sup>90</sup> Th	Pa	92 U	93 Np	94 Pu	<sup>95</sup> Åm	<sup>96</sup> Cm	97 Bk	98 Cf	<sup>99</sup> Es	100 Fm	Md	102 No	103 Lr

Anomalous Neutron Diffraction of Disordered Materials R Sinclair. World Scientific p107. ISBN 981-02-1463-4.







## Reverse Monte Carlo Modeling of Neutron and X-ray data



Best (essential ?) to use more than one structure factor plus chemical constraints



## **Empirical Potential Structure Refinement**

#### Quantum isotope effects in water





## Molecular dynamics Simulations

0.04



#### Tetrahedral oxygen triclusters in Yttria-Alumina glasses

J. Phys.: Condens. Matter 21 (2009) 205102.



160

180



## Specialized Sample Environments : Levitator





#### Tmax =300°C. Supercool liquids several hundered degrees.



Phys. Rev. Lett., 98 (2007) 057802.



## Specialized Sample Environments : High Pressure



HDA

Phys. Rev. Lett., 97 (2006) 115503. Science 297 (2002) 1320.







### Time Resolved Measurements : Chemical Reactions



Courtesy of Eugene Bychkov







## Last slide





**Chris's PDF guidelines** Real space peak position = bond length Peak area  $\alpha$  coordination number Model disagrees with data = it's wrong! No peaks = no atoms

